

# Superfluid turbulence in rotating $^3\text{He-B}$

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# Overview

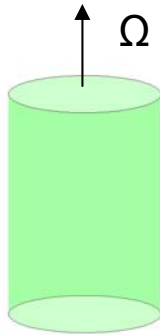
- Introduction to the experiment
- Experimental observations on:
  - Criteria for turbulence
  - Sequence of events

$^3\text{He}$  compared to  $^4\text{He}$ :

- High viscosity of normal component
- NMR
- Range of mutual friction
- Vortex formation different

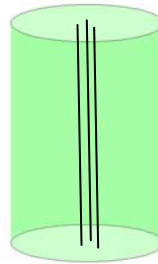
# Vortex states

vortex-free rotation



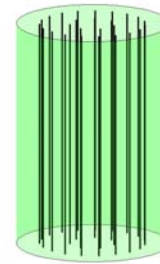
- maximum energy state
- normal component in corotation with the bucket
- superfluid stationary in laboratory frame

intermediate



- $0 < N < N_{\max}$

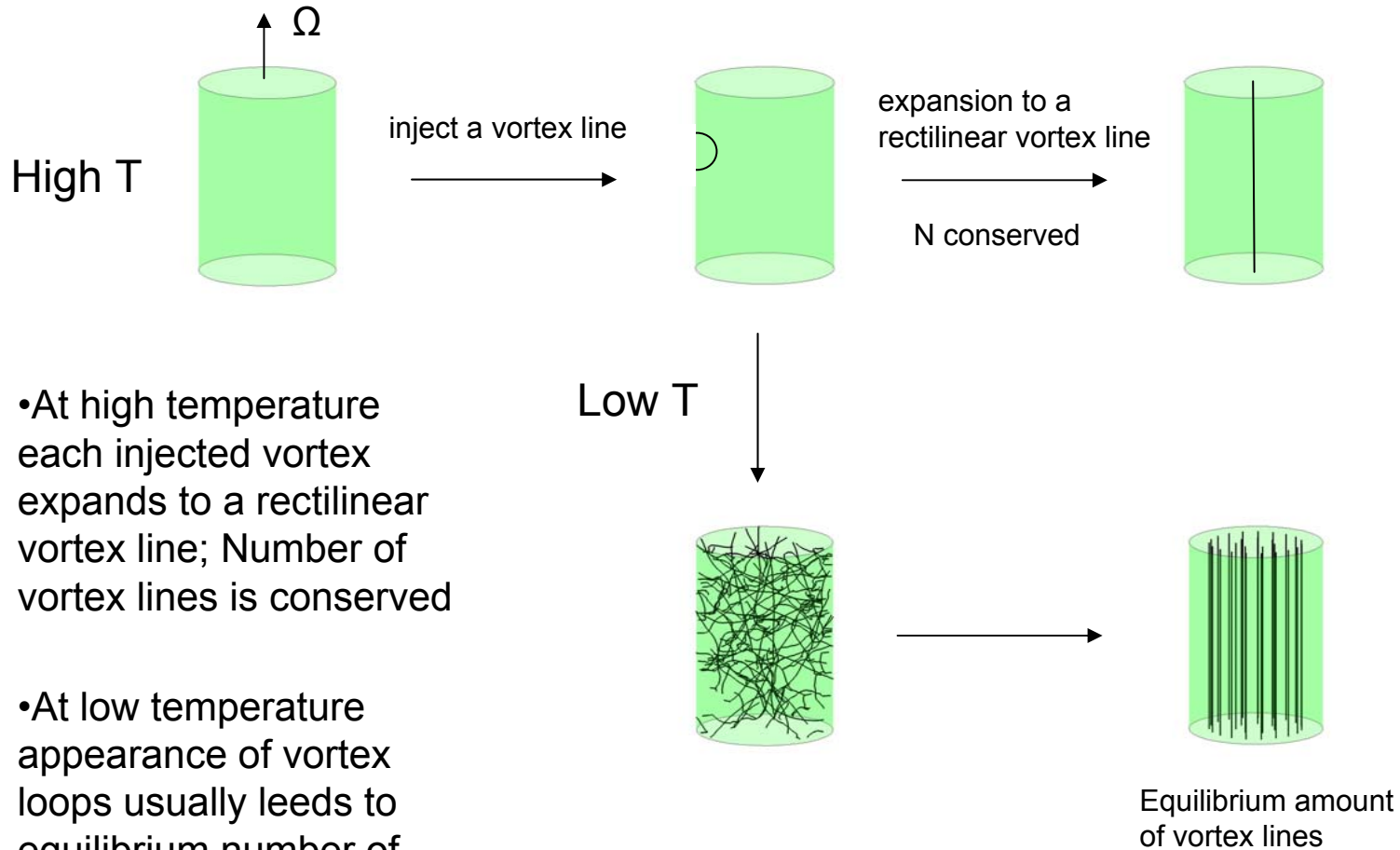
solid-body rotation



- minimum energy state
- superfluid mimics solid-body rotation
- total number of vortex lines:

$$N = \pi R^2 \frac{2\Omega}{\kappa}$$

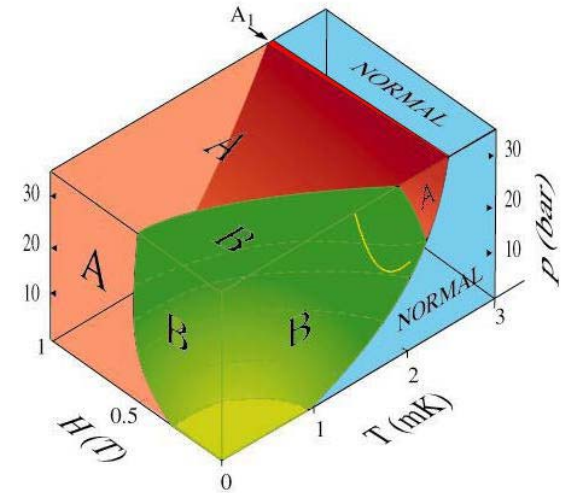
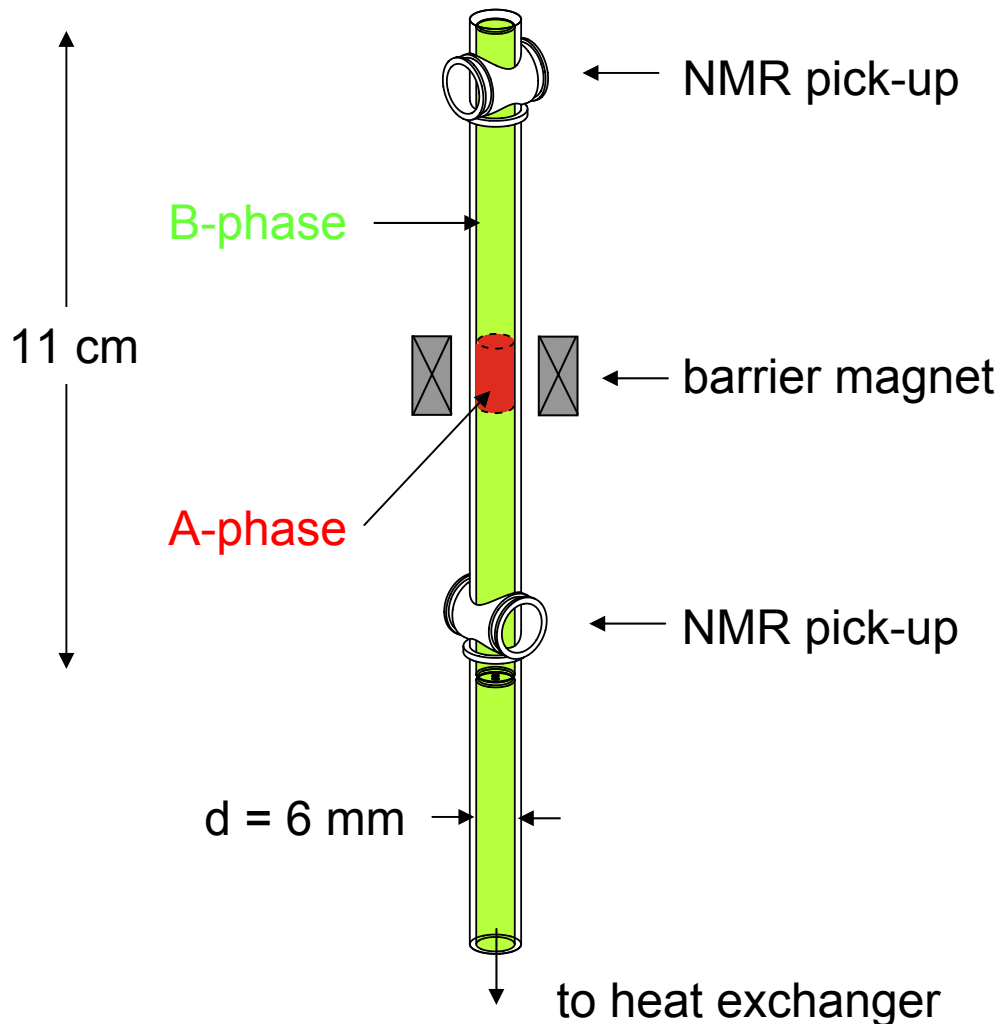
# Overview of the Experiment



- At high temperature each injected vortex expands to a rectilinear vortex line; Number of vortex lines is conserved

- At low temperature appearance of vortex loops usually leads to equilibrium number of vortex lines

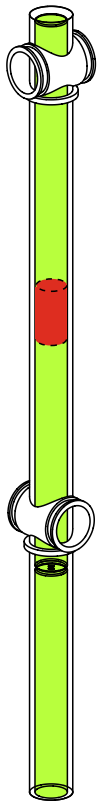
# Experimental setup



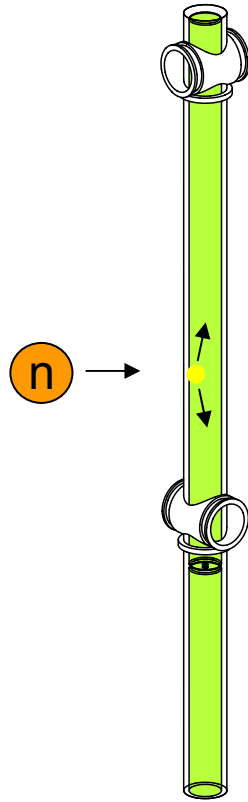
- Rotation up to  $4 \text{ rad/s}$
- Magnetically stabilized AB phase boundary for vortex line injection

# Mechanisms for vortex formation

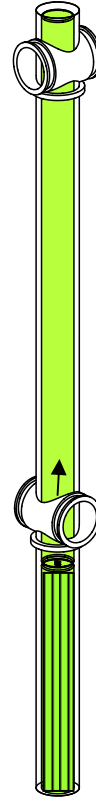
Shear-flow instability  
of AB interface



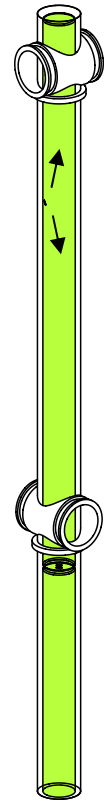
Kibble-Zurek  
after neutron capture



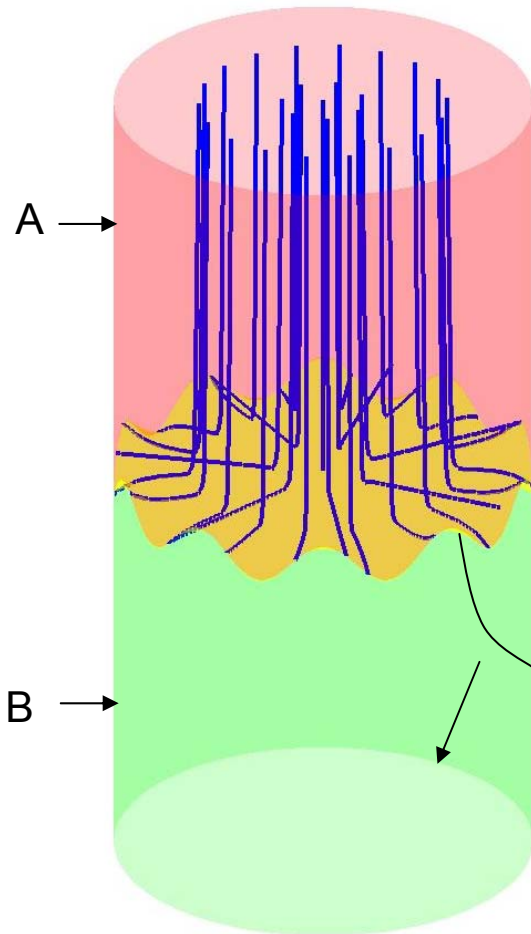
Flow through  
orifice



Wall defect

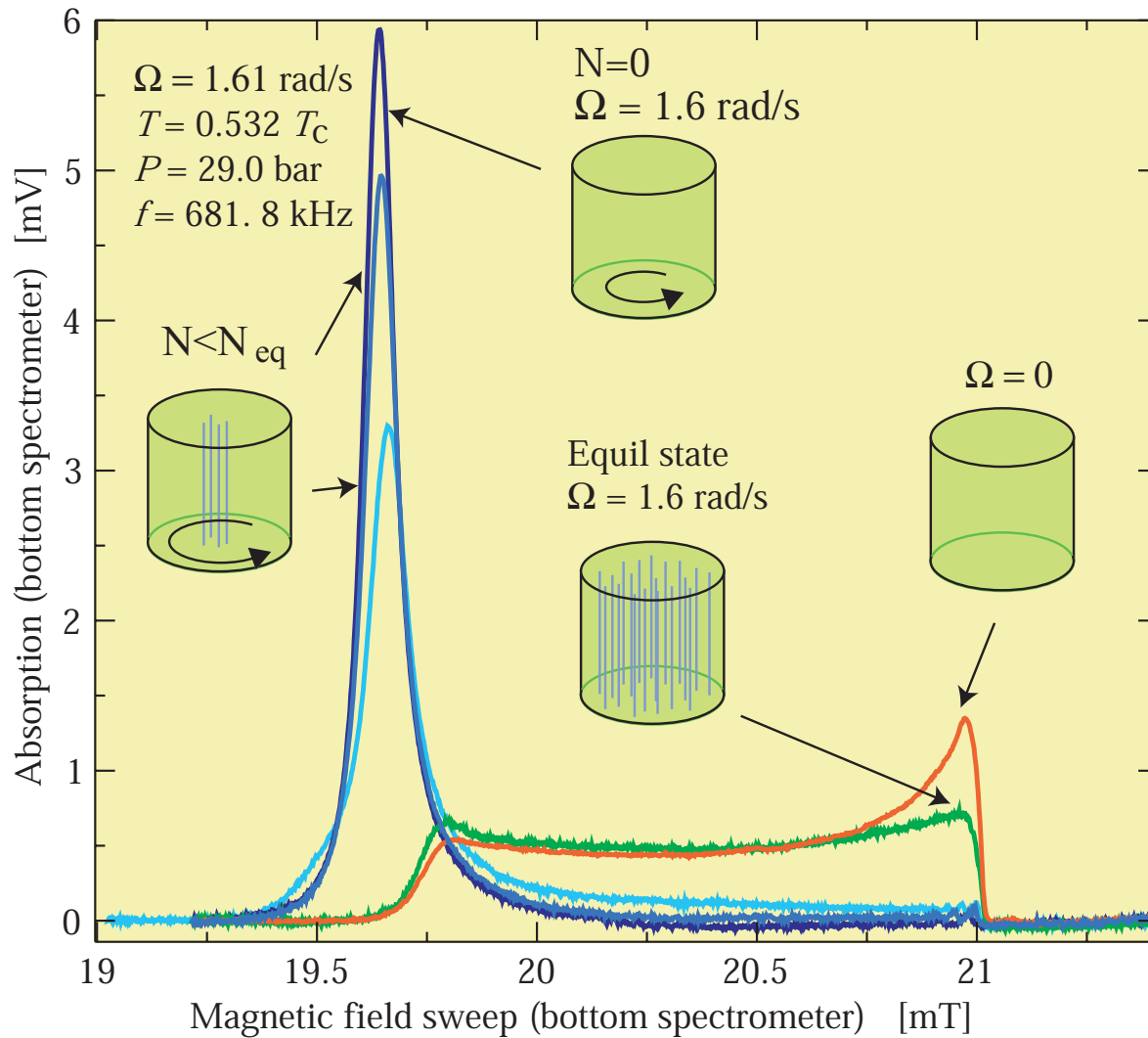


# Shear-flow instability of the AB phase boundary



- A phase has low  $\Omega_c$  and B phase high  $\Omega_c$ 
  - A mimics solid body rotation
  - B does not move
- Under rotation a velocity difference between the superfluids form, "wind"
- Phase boundary becomes unstable and vortex lines are injected to the B phase
- Number of vortex lines injected  $N \sim 10$
- Velocity where vortex lines are injected can be tuned with magnetic field

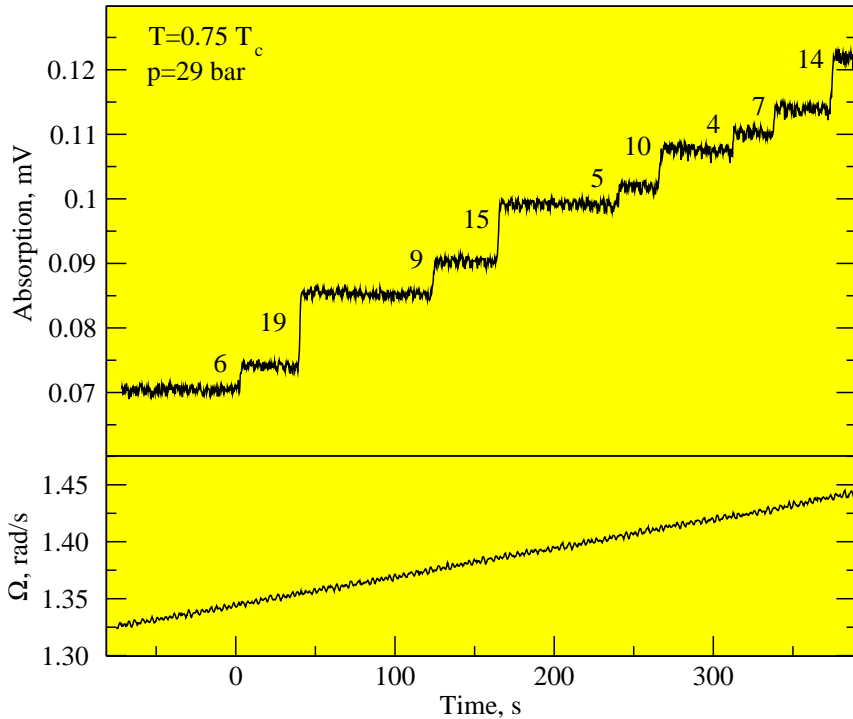
# NMR on $^3\text{He-B}$



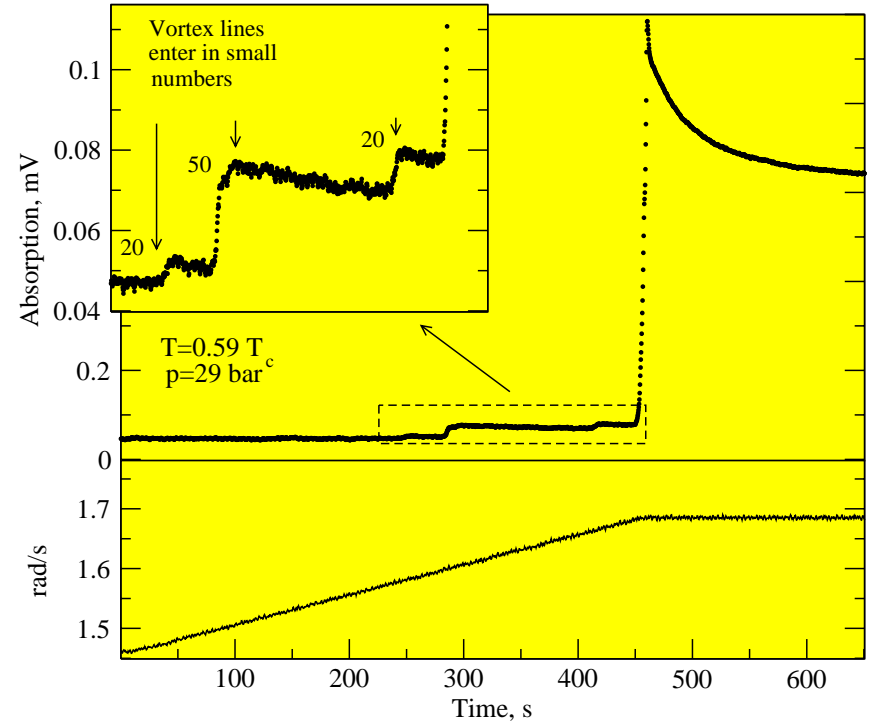


# Vortex formation at high T

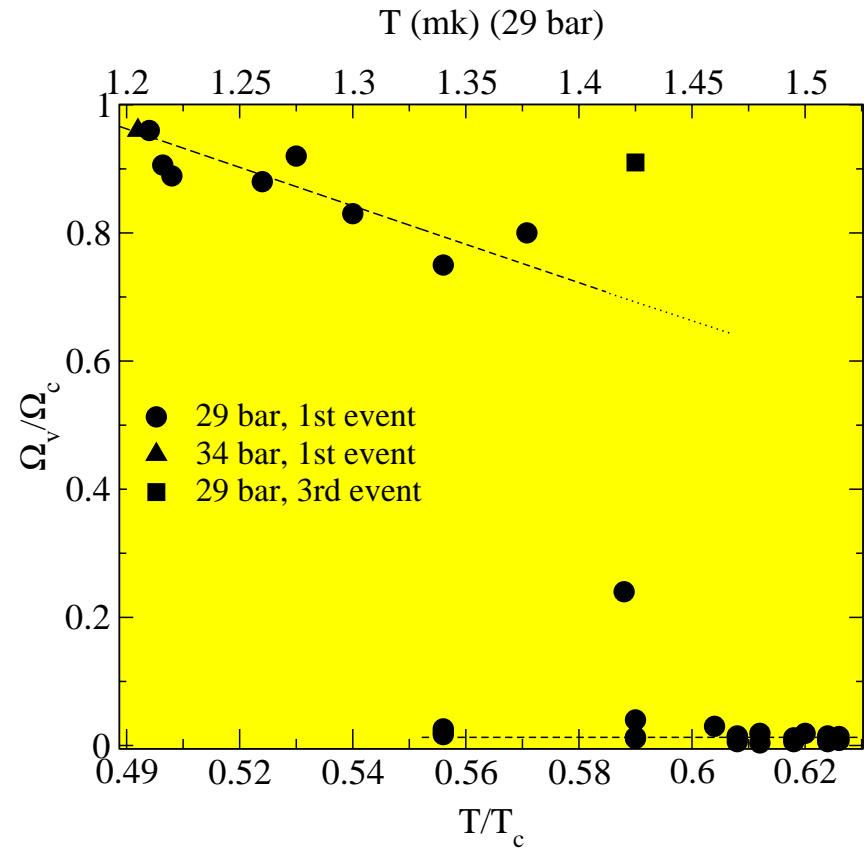
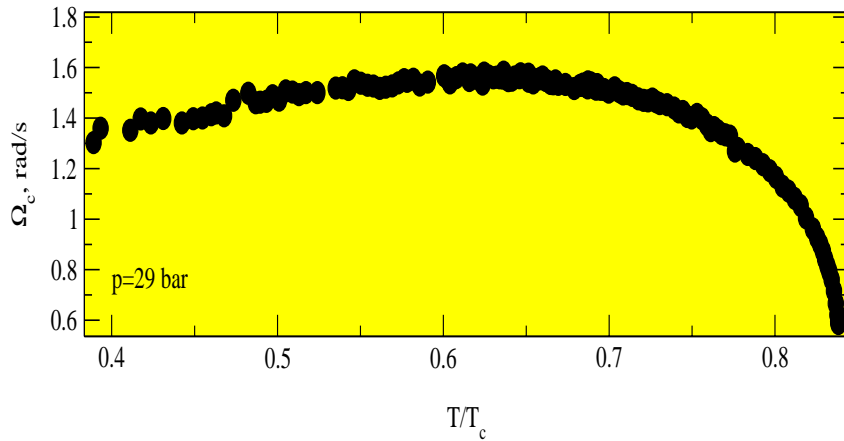
High T



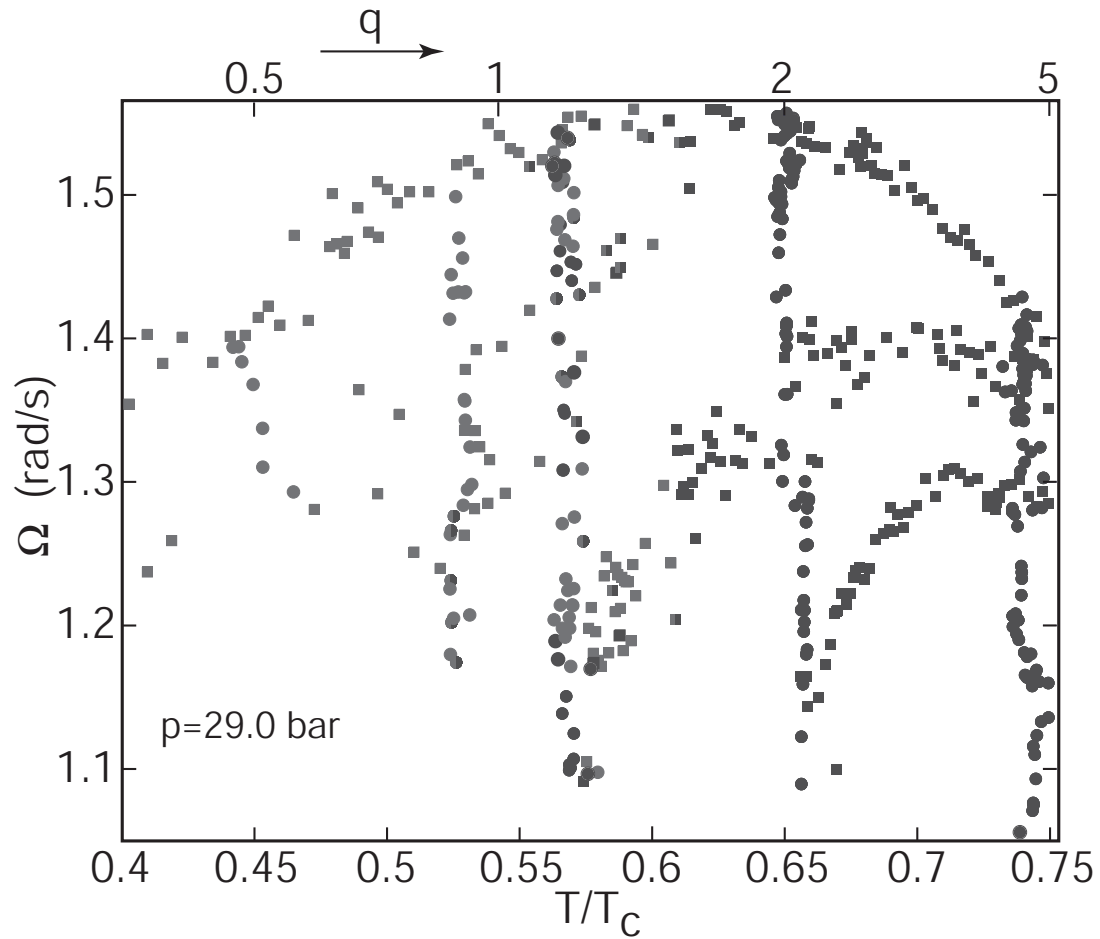
Low T



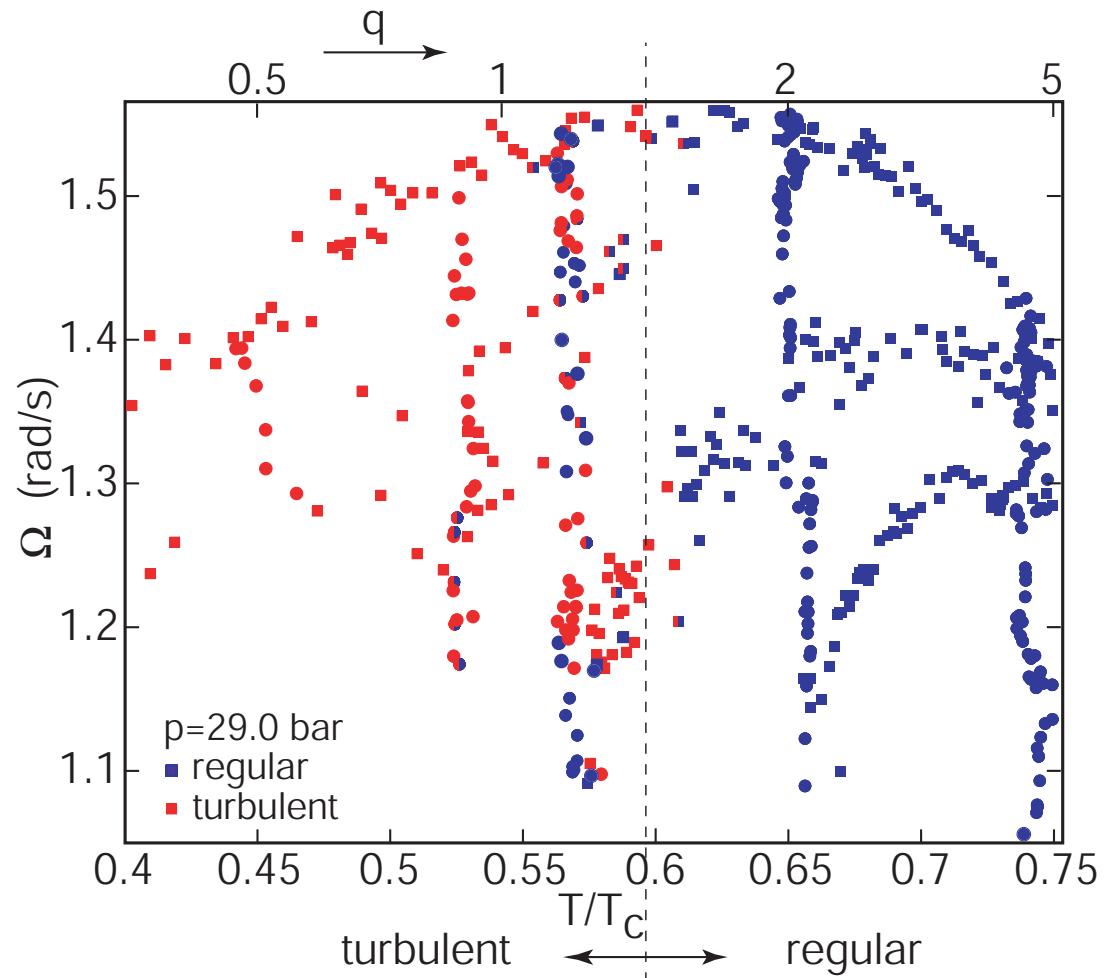
# Number of vortex lines per event as a function of T



# Transition to turbulence



# Transition to turbulence



# Discussion

For classical liquids, taking  $\omega = \nabla \times v$

$$\frac{\partial \omega}{\partial t} = \nabla \times [v \times \omega] + \nu \nabla^2 \omega$$

inertial  $\sim U\omega/R$

viscous  $\sim \nu\omega/R^2$

$$\frac{\text{inertial}}{\text{viscous}} = Re = UR/\nu > 1 \rightarrow \text{turbulence}$$

For superfluids with  $v_n=0$ ,  $Re_s=UR/\kappa > 1$  and  $\omega_s = \langle \nabla \times v_s \rangle$  averaged over vortex lines

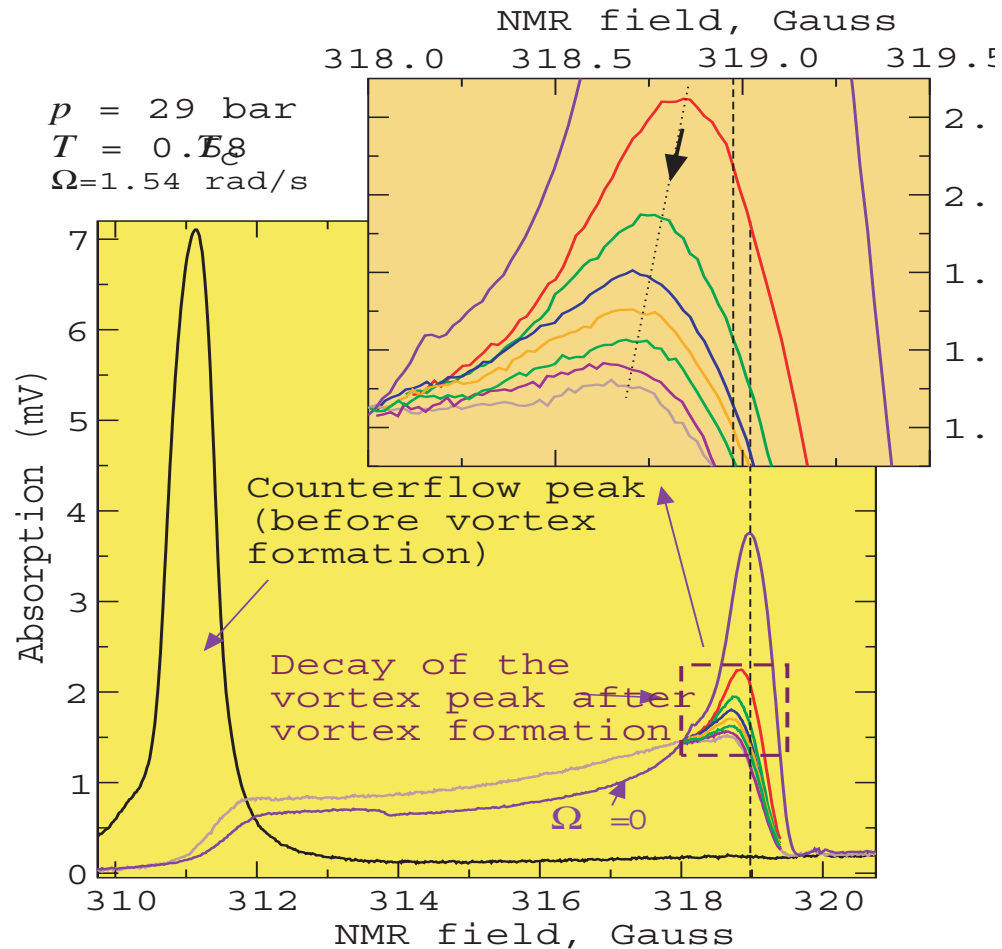
$$\frac{\partial \omega_s}{\partial t} = (1-\alpha') \nabla \times [v_s \times \omega_s] + \alpha \nabla \times [\hat{\omega}_s \times (\omega_s \times v_s)]$$

inertial  $\sim (1-\alpha')U\omega/R$

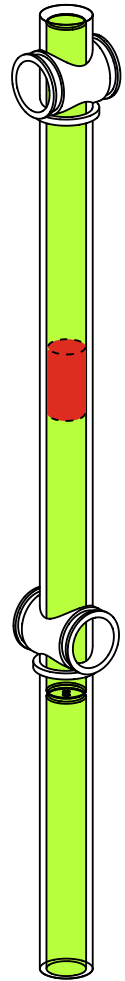
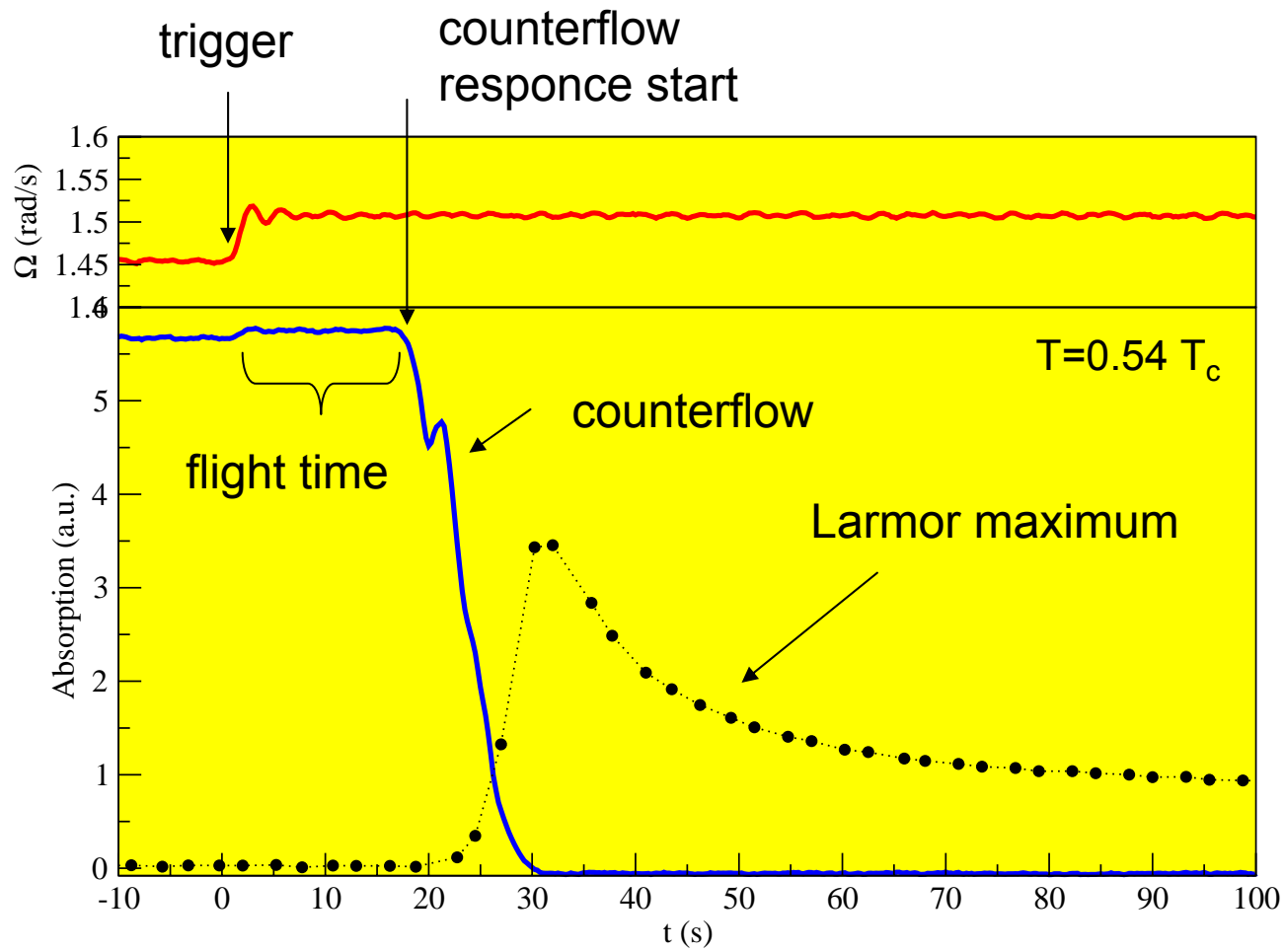
viscous  $\sim \alpha U\omega/R$

$$\frac{\text{inertial}}{\text{viscous}} = \frac{1-\alpha'}{\alpha}$$

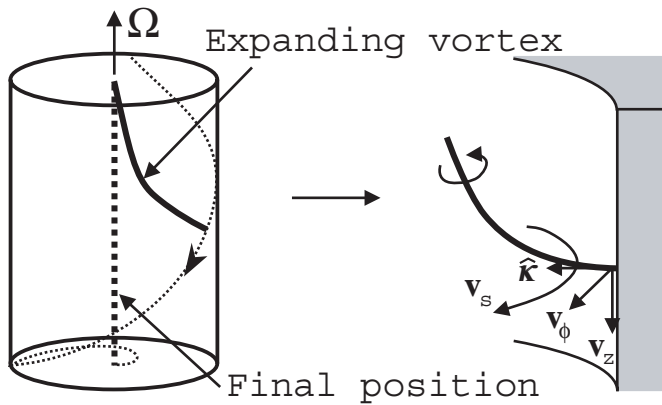
# Spectra of turbulent events



# Timing

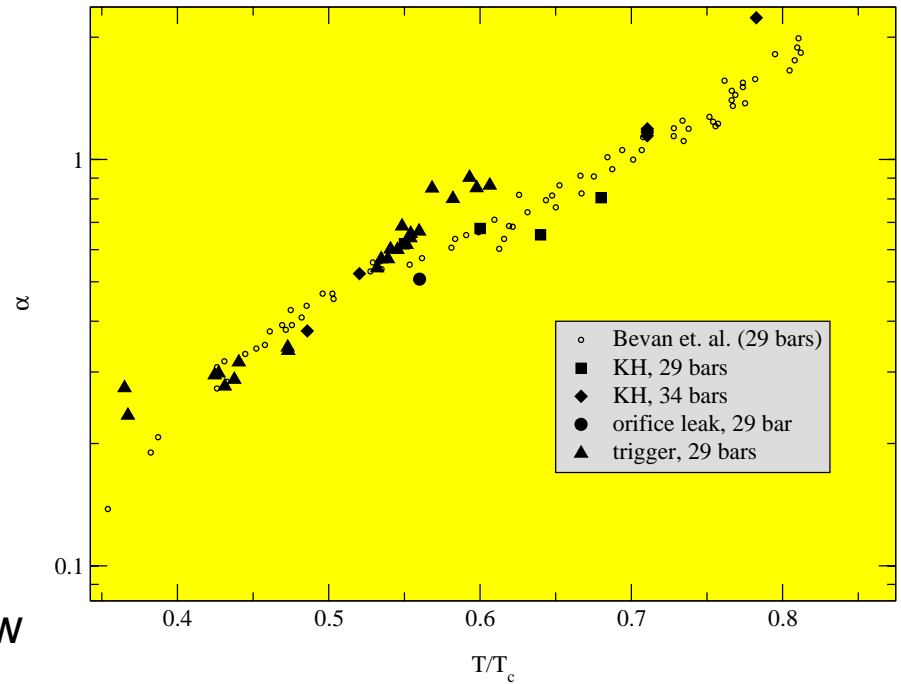


# Flight time



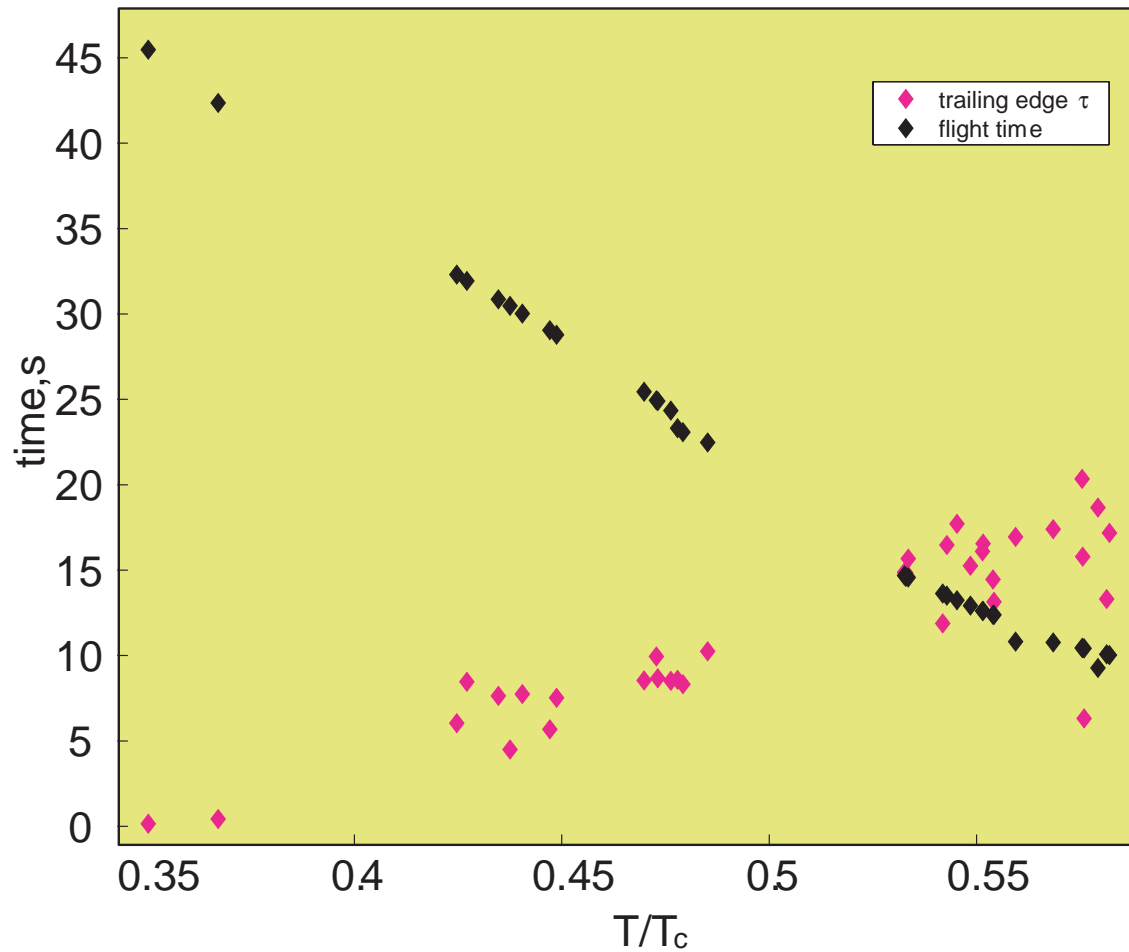
- The speed at which the turbulence expands to the vortex free counterflow

$$v_z = \Omega R \alpha$$

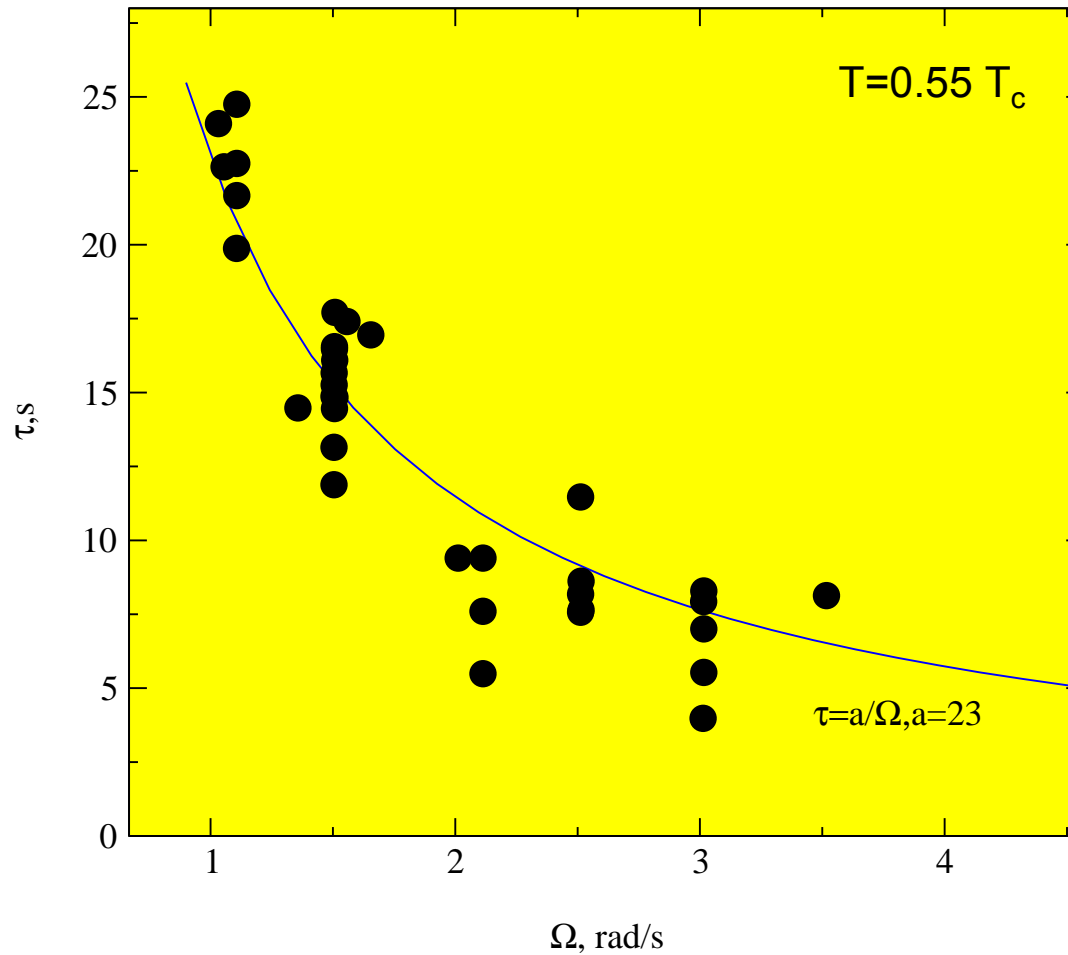




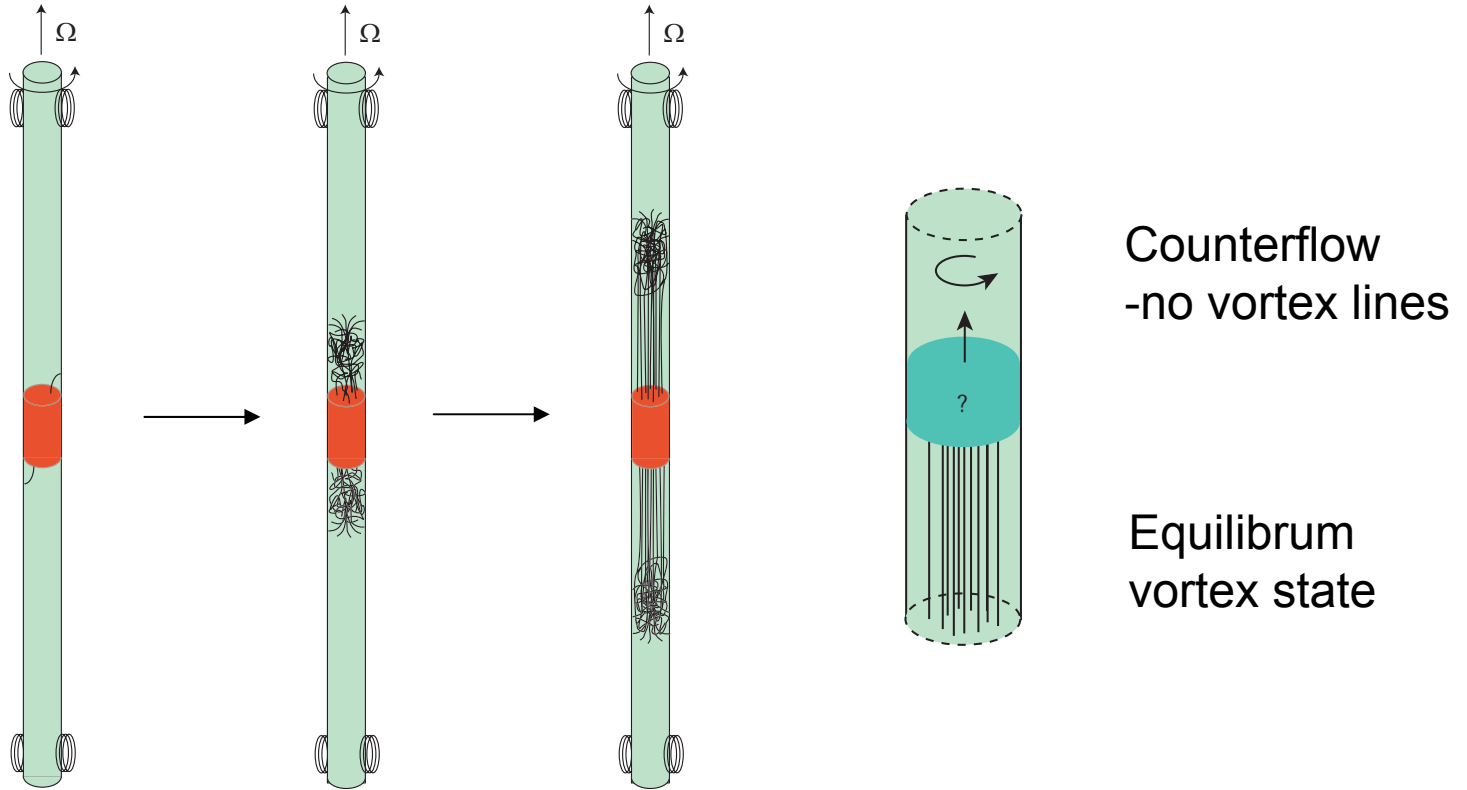
# Trailing edge $\tau$ as a function of $T$



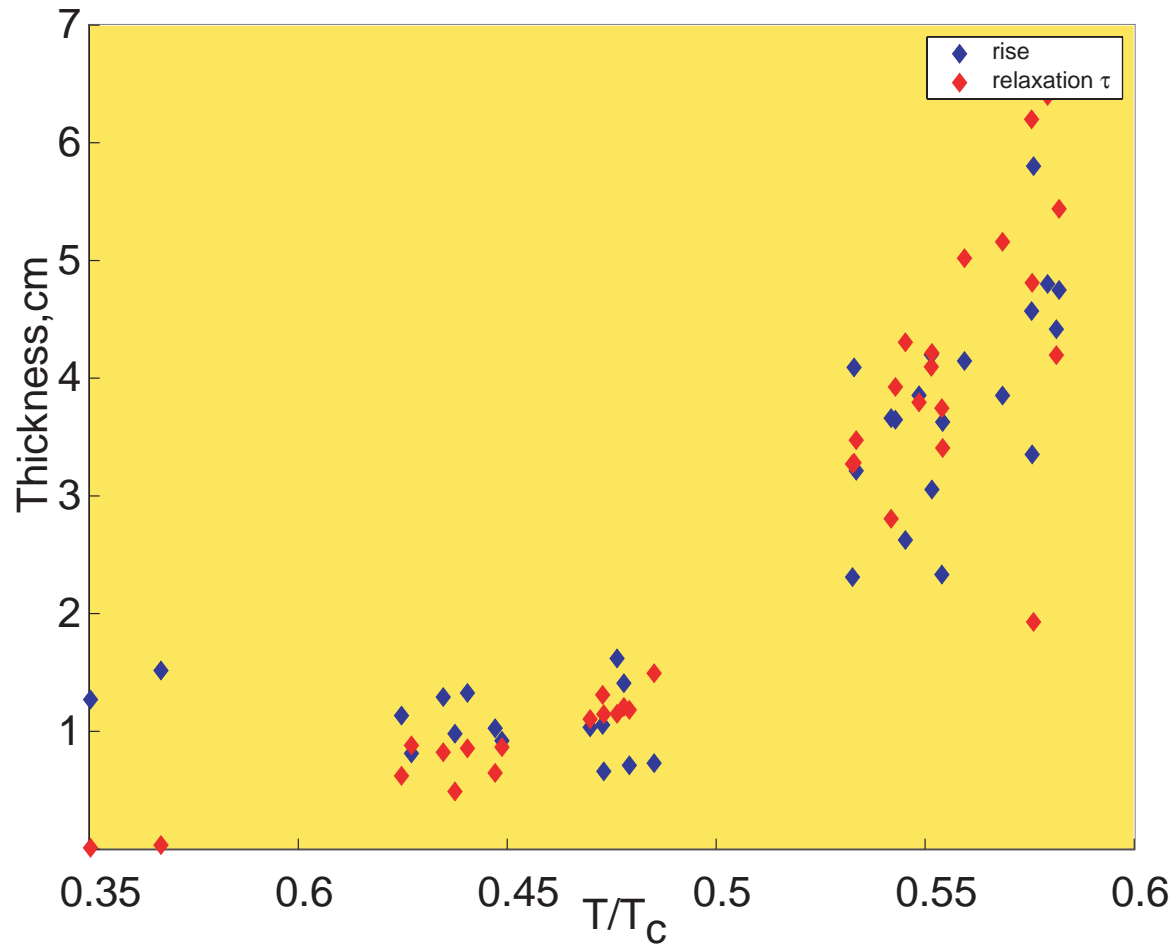
# Trailing edge $\tau$ as a function of $\Omega$



# Experiment in scale



# Layer thickness



# Conclusions

- Two clear regimes in  $^3\text{He-B}$ : laminar and turbulent
- In our experiment we see a "turbulent layer" propagating through the sample
- Why does the trailing edge  $\tau$  decrease towards lower  $T$ ?